REPORT DOCUMENTATION PAGE

Form Approved OMB No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing this collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden to Department of Defense, Washington Headquarters Services, Directorate for Information Operations and Reports (0704-0188), 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302. Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to any penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number. PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ADDRESS.

2. REPORT TYPE	3. DATES COVERED (From - To)		
Briefing Charts	Mar 2014- June 2014		
	5a. CONTRACT NUMBER		
	In-House		
-layer flow with gas injection	5b. GRANT NUMBER		
	5c. PROGRAM ELEMENT NUMBER		
	5d. PROJECT NUMBER		
dakov; Ivett A Leyva	5e. TASK NUMBER		
	5f. WORK UNIT NUMBER Q0AF		
E(S) AND ADDRESS(ES)	8. PERFORMING ORGANIZATION REPORT NO.		
IC)			
CY NAME(S) AND ADDRESS(ES) (IC)	10. SPONSOR/MONITOR'S ACRONYM(S)		
	11. SPONSOR/MONITOR'S REPORT		
	NUMBER(S)		
	AFRL-RQ-ED-VG-2014-149		
	Briefing Charts -layer flow with gas injection dakov; Ivett A Leyva E(S) AND ADDRESS(ES) 1C) CY NAME(S) AND ADDRESS(ES)		

12. DISTRIBUTION / AVAILABILITY STATEMENT

Distribution A: Approved for Public Release; Distribution Unlimited

13. SUPPLEMENTARY NOTES

Briefing Charts presented at 44th AIAA Fluid Dynamics Conference, Atlanta, GA, 16-20 June 2014. PA#14289

14. ABSTRACT

Stability analyses of high-speed boundary-layer flow past a 5° half angle sharp cone with the wall-normal injection of air through a porous strip are performed using Navier-Stokes solutions for the mean flow and linear stability theory. The configuration and free-stream parameters are chosen to be similar to the experiments, which were carried out at Caltech's T5 shock tunnel to investigate the effect of CO₂ injection on laminar-turbulent transition. The analysis is focused on pure aerodynamic effects in the framework of perfect gas model. It is shown that the injection leads to destabilization of the Mack second mode in the nearfield relaxation region and its stabilization in the far-field relaxation region. To reduce the destabilization effect it was suggested to decrease the injector surface slope or use suction-blowing of zero net injection. However, the eⁿ computations showed that these modifications did not improve the injector performance in the near-filed region in general. For special cases of low injection rates in which the N-factors in the near field region are below the critical level, shaping can produce a significant stabilization in the mid- and far-field regions.

15. SUBJECT TERMS

16. SECURITY CLAS	SIFICATION OF:		17. LIMITATION OF ABSTRACT	18. NUMBER OF PAGES	19a. NAME OF RESPONSIBLE PERSON Ivett Leyva
a. REPORT	b. ABSTRACT	c. THIS PAGE	SAR	51	19b. TELEPHONE NO (include area code)
Unclassified	Unclassified	Unclassified			661-275-5817



Stability analysis of high-speed boundary-layer flow with gas injection

Alexander Fedorov and Vitaly Soudakov

Moscow Institute of Physics and Technology

Ivett A. Leyva

Air Force Research Laboratory, Edwards AFB

7th AIAA Theoretical Fluid Mechanics Conference June 16-20, 2014, Atlanta, Georgia

This work was supported by the European Office of Aerospace Research and Development via the US Civilian Research and Development Foundation, grant CRDF-31107-MO-12







Outline

- Background and motivation
- Baseline configuration and numerical approach
- Stability analysis for the baseline configuration
 - Mean flow
 - Acoustic instabilities
 - N-factors
- How to improve the injector performance
- Shaping of injector
 - Conical shapes
 - Cylindrical shape
- Suction-blowing of zero mass injection
- Conclusions







Background: Delay Transition Using Non-Equilibrium CO₂ to Suppress the Second Mode

PROBLEM: In hypersonic flight, heating loads are typically a dominant design factor

Turbulent heat transfer rates can be about an order of magnitude higher than laminar rates at hypersonic Mach numbers

A reduction in heating loads by keeping the boundary layer laminar longer means less thermal protection needed and hence less weight to carry, or conversely more payload deliverable for a given thrust.

OBJECTIVE: Delay transition from laminar to turbulent flow in the boundary layer of a slender hypersonic body by using nonequilibrium CO₂

Transition in high Mach numbers occurs through the Mack mode – amplification of acoustic waves traveling in the boundary layer

Molecular vibration and dissociation damp acoustic waves



At relevant conditions, CO₂ absorbs most energy at the frequencies most strongly amplified by 2nd (Mack) mode







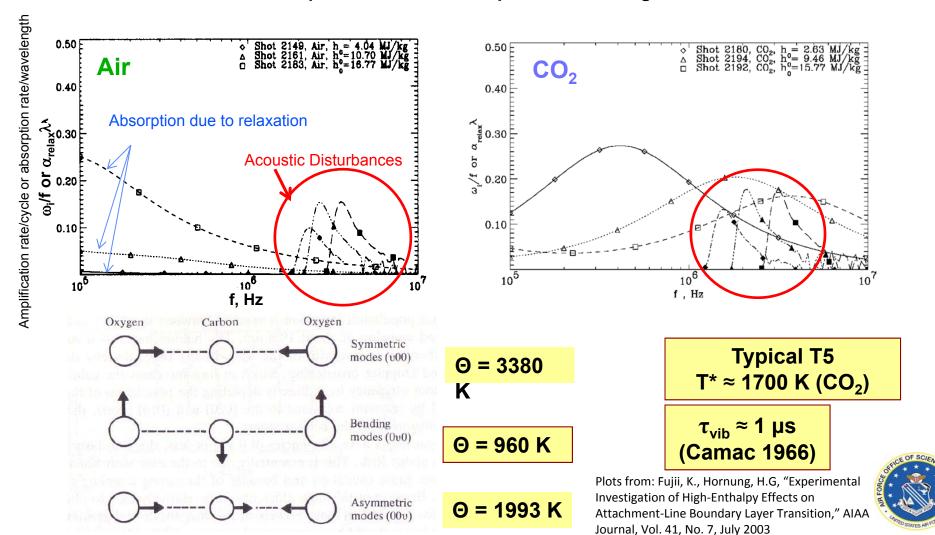
Inject CO₂ to delay transition in air flows of interest





Background

- For CO₂ the broad sound absorption curve peak coincides with the amplification peaks
- This coincidence is most pronounced at enthalpies of ~10 MJ/kg

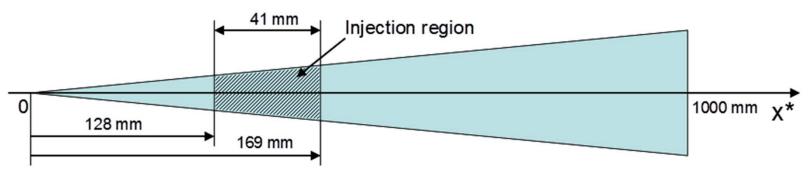




Baseline configuration

Free-stream parameters correspond to Run 2540* in GALCIT T5 shock tunnel

$$\begin{array}{lll} {\rm M}_{_{\infty}} = 5.3 & \rho_{_{\infty}}^* = 0.05788 \ {\rm kg/m^3} \\ T_{_{\infty}}^* = 1323.77 \ {\rm K} & U_{_{\infty}}^* = 3866 \ {\rm m/s} & \mu_{_{\infty}}^* = 4.897 \times 10^{-5} \ {\rm Pa \cdot s} \\ p_{_{\infty}}^* = 21993 \ {\rm Pa} & T_{_{w}}^* = 293 \ {\rm K}, \ T_{_{w}}^* / T_{_{\infty}}^* = 0.22 & L^* = 1 \ {\rm m} \end{array}$$



5-deg half-angle sharp cone with the injector

Gas is injected with the total mass flow rate ranging from 3 g/s to 13.5 g/s





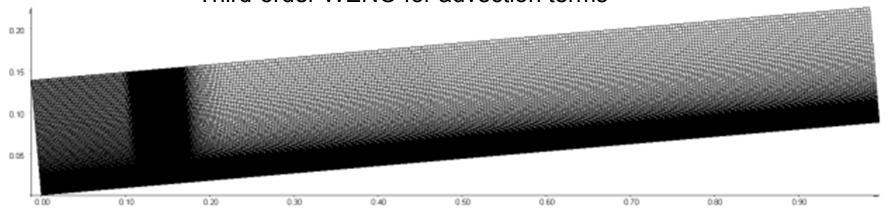
^{*}Parameters are determined using M_{∞} , T_{∞} , and ρ_{∞} reported by Wagnild, R.M. et al. (AIAA-2010-1244) and perfect-gas model with Pr=0.72 and γ =1.4



Numerical approach for mean flow

In-house Navier-Stokes code HSFlow*

- Perfect gas of Pr=0.72, γ =1.4
- Sutherland viscosity-temperature dependence
- Implicit second-order finite-volume method
- Shock-capturing scheme
- Third-order WFNO for advection terms



597×649 grid with

- 50% clustering in the boundary layer
- Clustering near the injector

^{*}Egorov, I.V. et al., Theor. Comput. Fluid Dyn., Vol. 20, No. 1, 2006, pp. 41-54.







Stability analysis

Local-parallel stability computations

- Third-order Rungge-Kutta scheme for integration of stability equation
- Gramm-Schmidt orthogonalization procedure
- Eigenvalues are calculated using a shooting/Newton-Raphson procedure

Disturbance~
$$\mathbf{q}(y) \exp(i\alpha x + i\beta z - i\omega t)$$

For temporal problem $\omega(\alpha, \beta, x)$ is complex, growth rate= ω_i

For spatial problem $\alpha(\omega,\beta,x)$ s complex, growth rate= $\sigma=-\alpha_{i}$

N-factors
$$N(x,\omega,\beta) = \int\limits_{x_0(\omega,\beta)}^x \sigma(\omega,\beta,x) dx$$



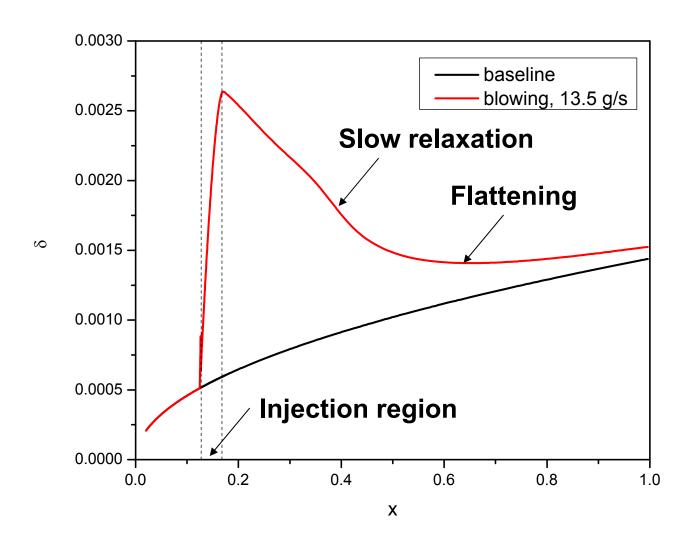


^{*}Egorov, I.V. et al., Theor. Comput. Fluid Dyn., Vol. 20, No. 1, 2006, pp. 41-54.



Boundary layer thickness

baseline configuration with injection rate=13.5 g/s

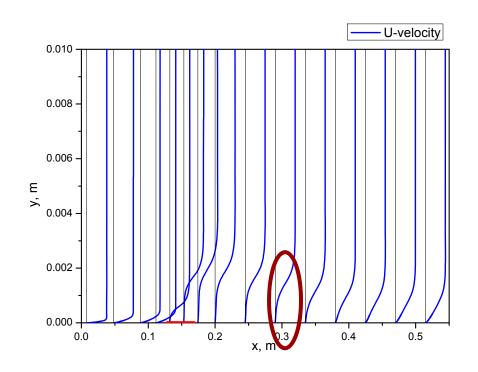


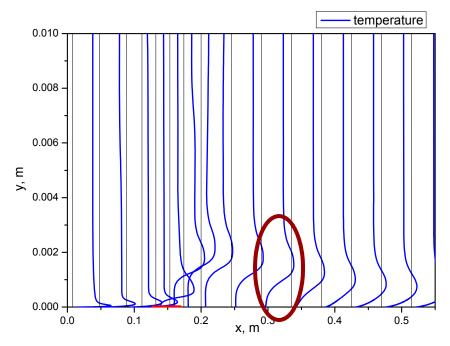






Mean-flow profiles





Baseline configuration with injection rate=13.5 g/s

- Thick region of cold dead flow near wall
- Slow relaxation downstream

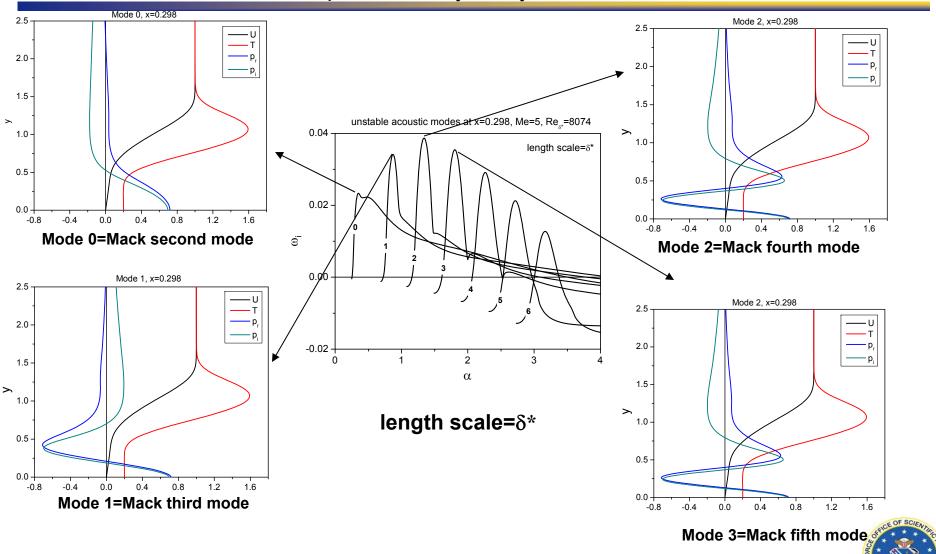






We are dealing with acoustic instability

Temporal stability analysis at x=0.3



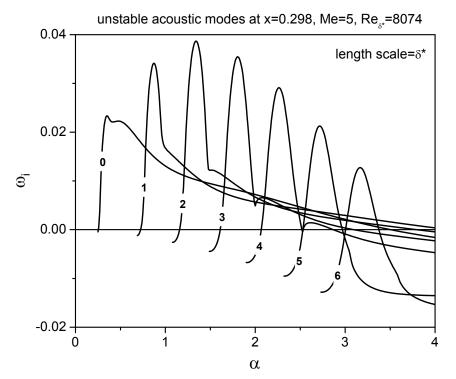


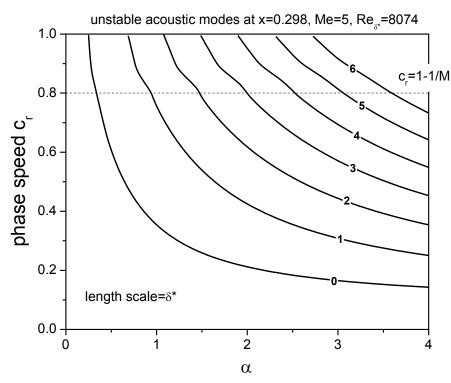


Temporal instability in the relaxation region for baseline configuration

(injection rate 13.5 g/s)



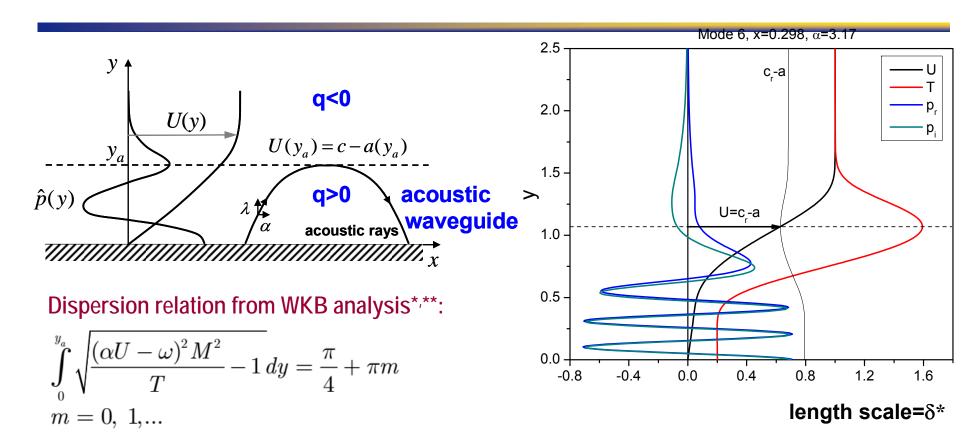




- •There are seven unstable modes!
- Mode 2 (Mack fourth mode) has maximal local increment



We are dealing with acoustic instability (cont'd)



Acoustic modes are formed in the waveguide between the wall (y=0) and the relative sonic line $y=y_a$: $U(y_a)=c_r-a(y_a)$

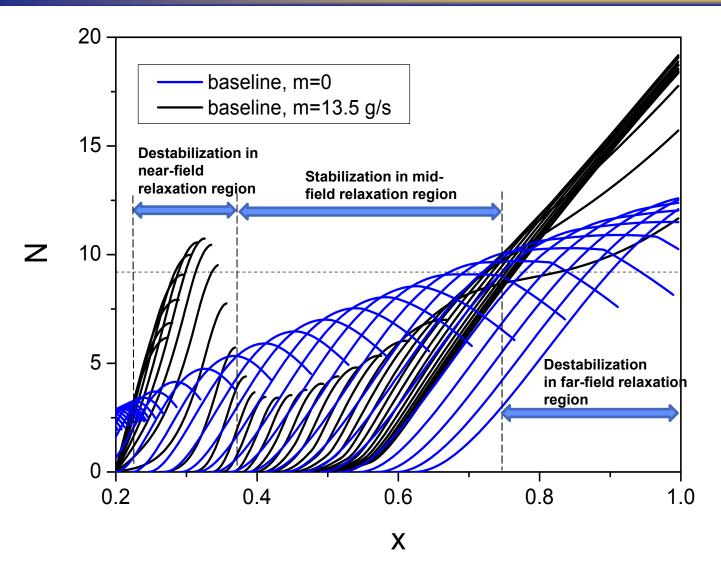


^{*}Guschin, V.R., & Fedorov, A.V., Fluid Dynamics, Vol. 24, No.1, 1989

^{**}Guschin, V.R., & Fedorov, A.V., NASA-TT-20683, April 1990



Injection affects N-factors of Mack second mode

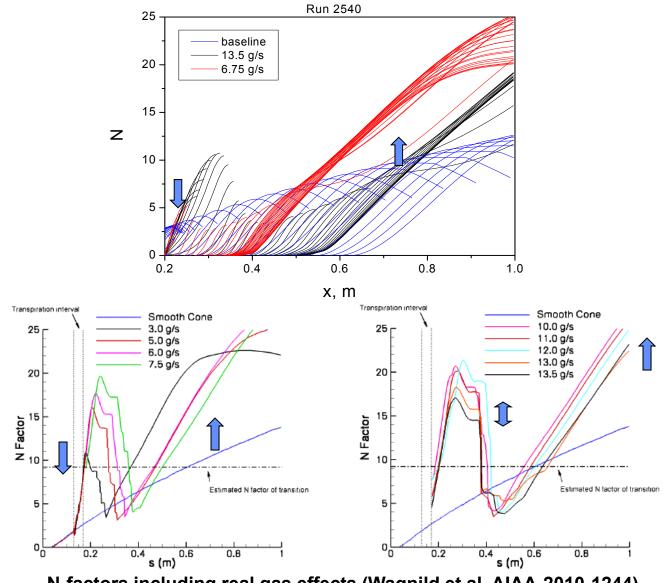








Perfect gas model captures basic trends





N-factors including real gas effects (Wagnild et al. AIAA-2010-1244)

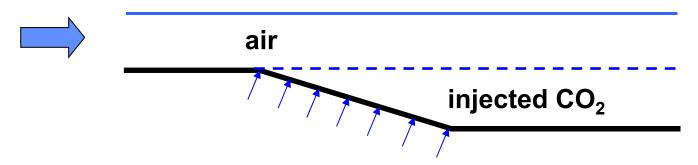
Distribution A: Approved for Public Release; Distribution Unlimited



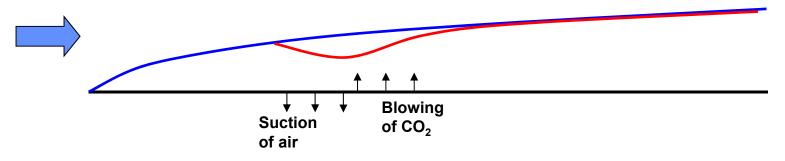


How to improve the injector performance?

 Negative slope may compensate the blowing effect on the displacement thickness



 Injection of zero total mass addition may help to reduce the relaxation region

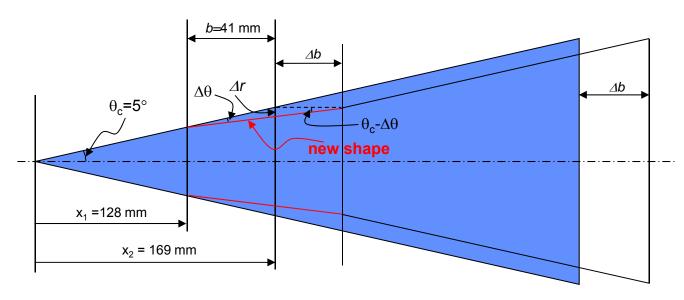








Injector of conical shape



5-deg half-angle sharp cone with the injector having the slope $\theta = \theta_c - \Delta \theta$

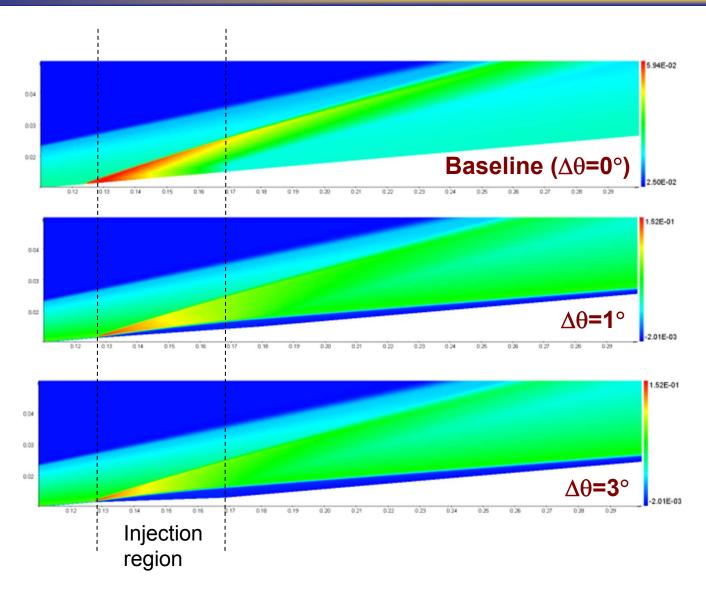
$$\begin{split} \Delta r &\approx b [\tan \theta_c - \tan(\theta_c - \Delta \theta)] \approx b \Delta \theta \\ \Delta b &= \frac{\Delta r}{\tan(\theta_c - \Delta \theta)} \approx \frac{\Delta r}{\tan \theta_c} \end{split}$$





Mean-flow pressure for conical injectors

(injection rate 13.5 g/s)



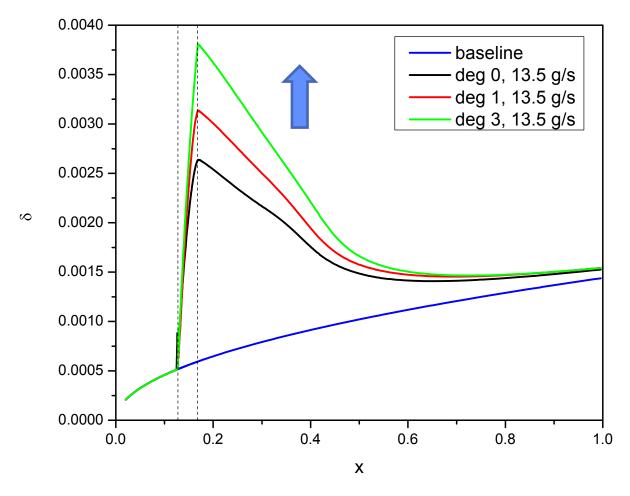






Mean-flow boundary layer thickness for conical injectors

(injection rate 13.5 g/s)



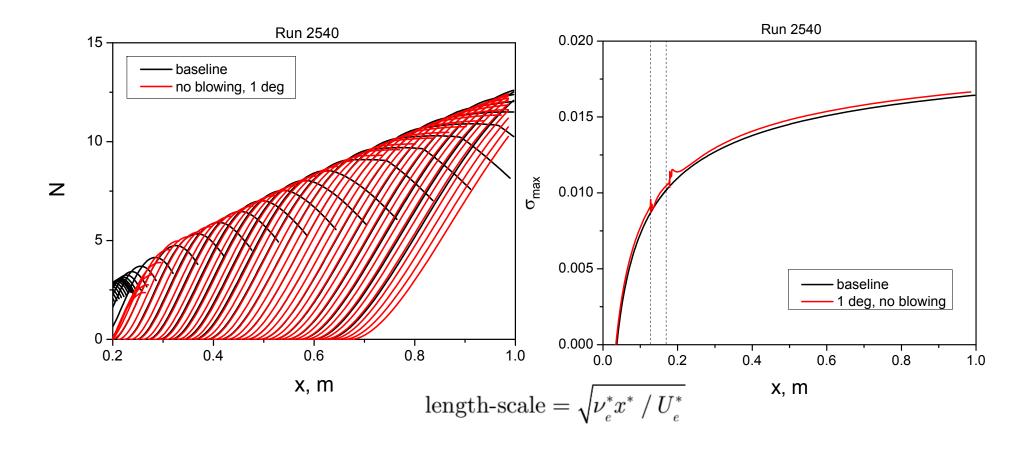
Boundary-layer thickness increases with $\Delta\theta$ in the relaxation region





THE AIR PORCE RESEARCH LANGRATORY

Shaping $\Delta\theta$ =1° without injection



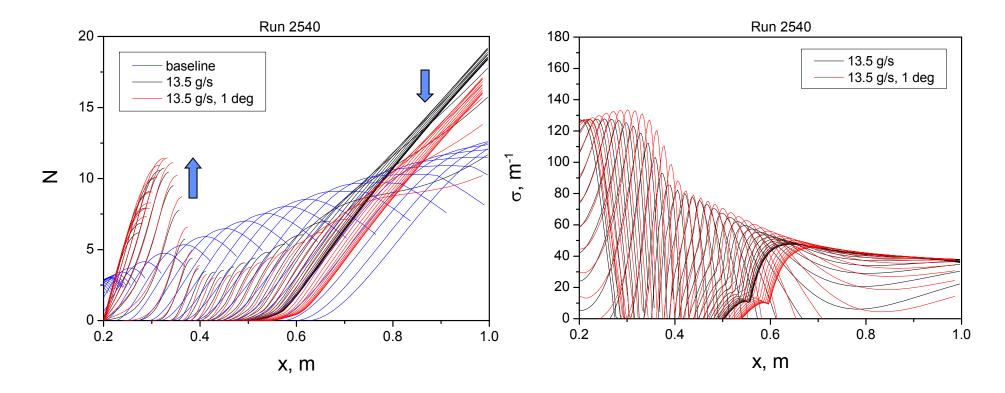
Effect of shaping is local and small







Shaping $\Delta\theta$ =1° with injection of 13.5 g/s



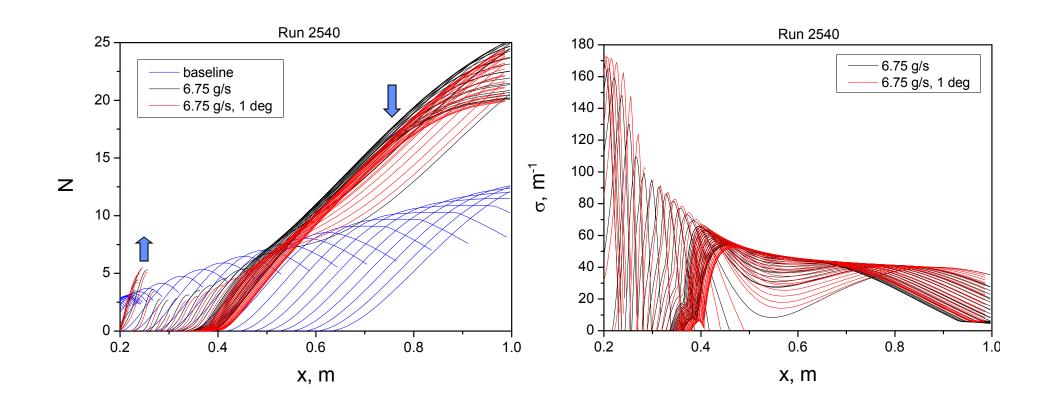
Conical injector with $\Delta\theta$ =1°

- Slightly destabilizes flow in the near-field relaxation region
- Slightly stabilizes flow in the far-field relaxation region





Shaping $\Delta\theta$ =1° and injection 6.75 g/s



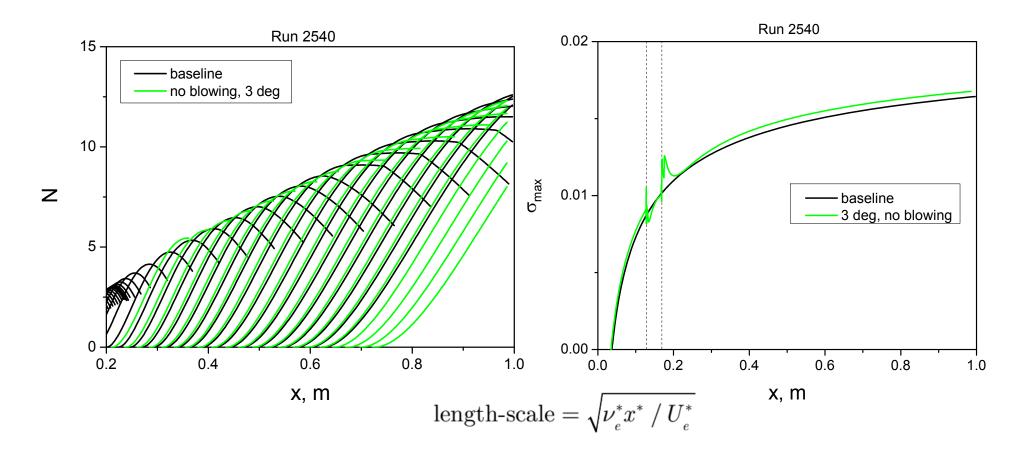
Shaping of $\Delta\theta$ =1° produces small effect on stability of flow at the injection rate 6.75 g/s







Shaping of $\Delta\theta$ =3° without injection



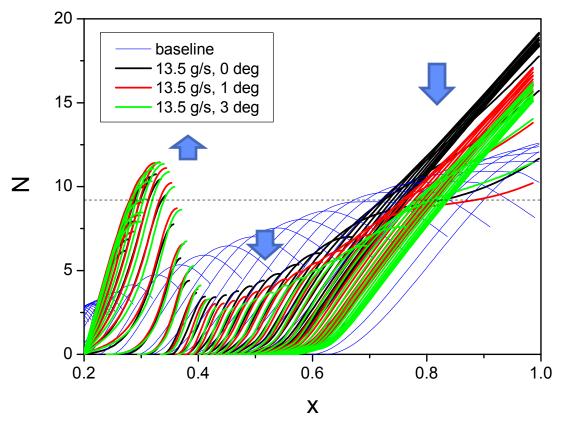
Effect of shaping is local and small







Summary plot of N-factors for conical injectors (injection rate 13.5 g/s)



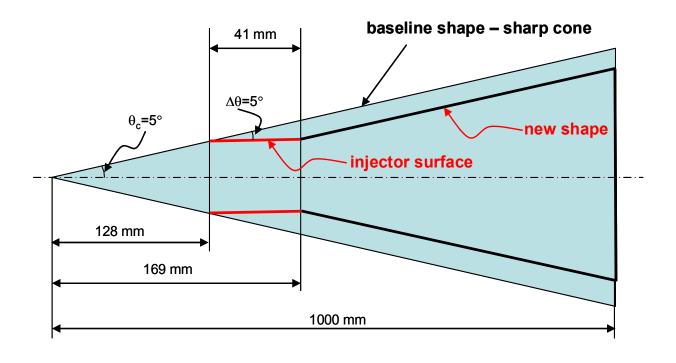
Shaping with $\Delta\theta$ =1° and 3°

- Slightly destabilizes flow in the near-field relaxation region
- Stabilizes flow in the far-field relaxation region





Injectors of cylindrical shape



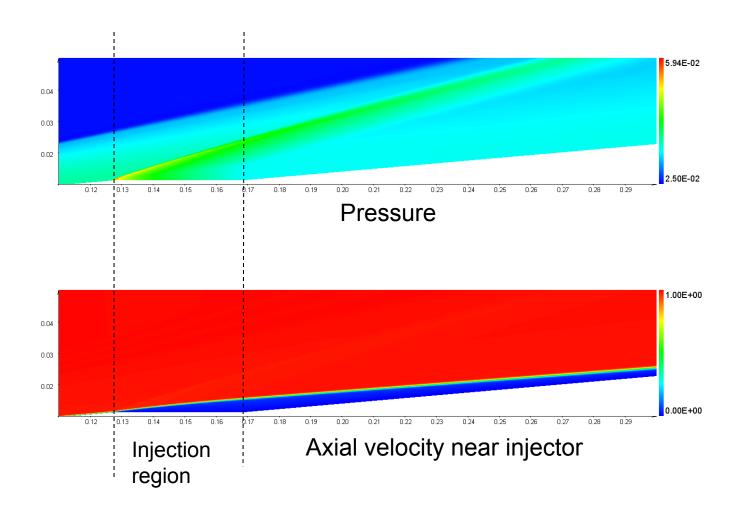






Mean flow for cylindrical injector

(injection rate 13.5 g/s)



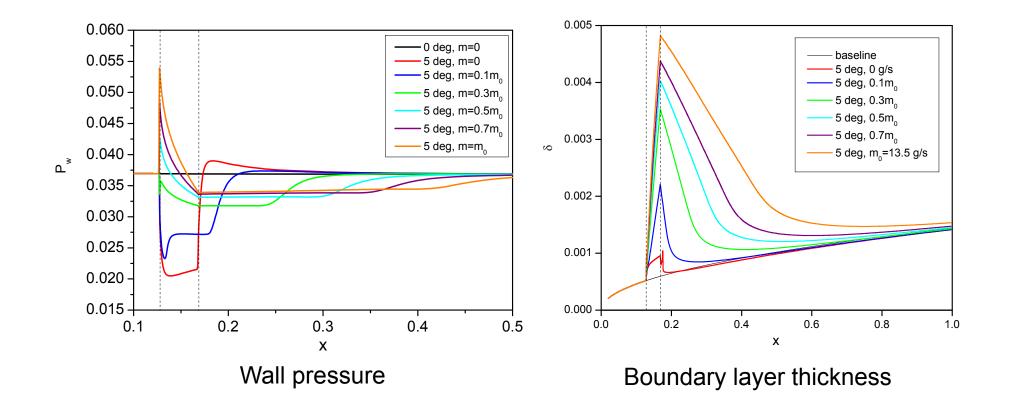






Mean flow for cylindrical injector

(various injection rates)

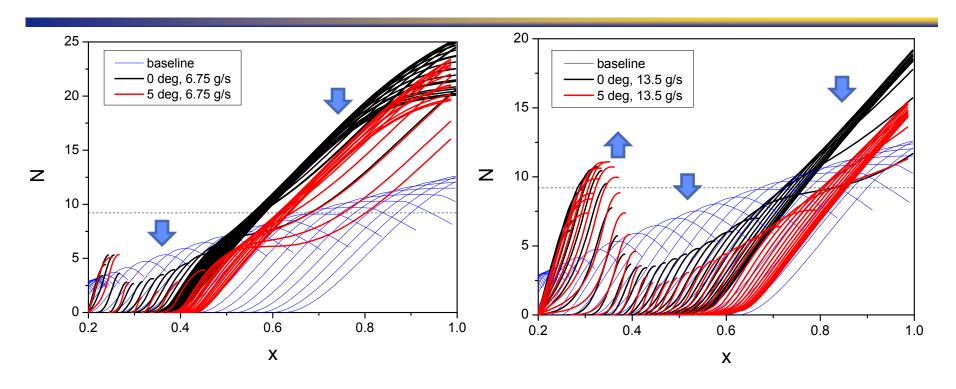








N-factors for cylindrical injector



This shaping

- Slightly destabilizes flow in the near-field relaxation region
- Stabilizes flow in the mid- and far-field relaxation region

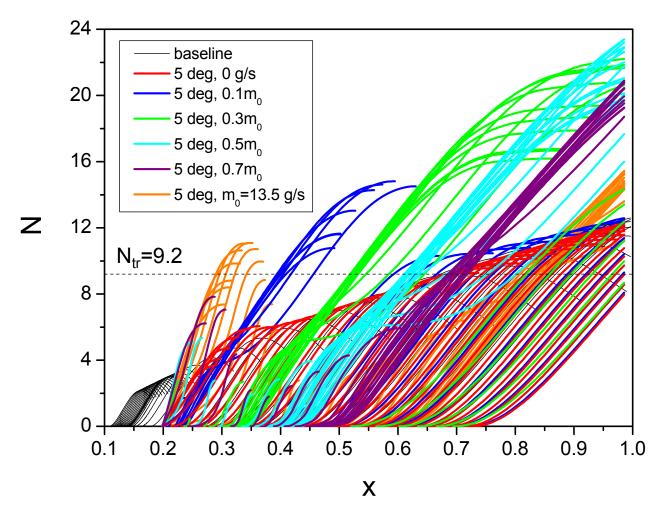






Summary plot of N-factors for cylindrical injector

(various injection rates)

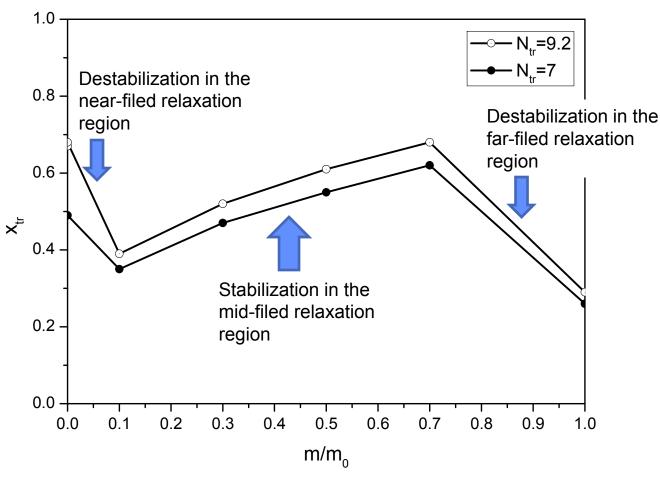


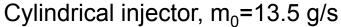






Estimates of the injection effect on the transition onset



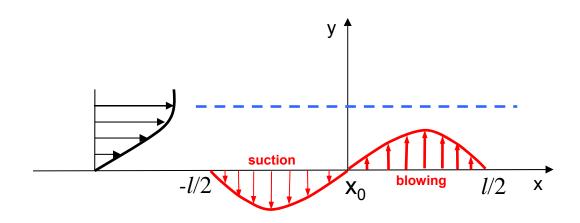








Suction-blowing of zero mass addition



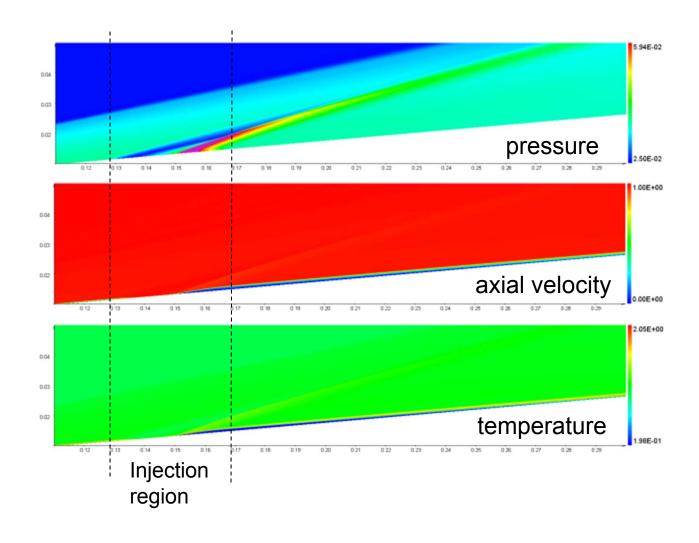
$$\begin{split} -l \, / \, 2 & \leq x - x_0 \leq l \, / \, 2 \\ z &= (x - x_0) 2\pi \, / \, l, \ -\pi \leq z \leq \pi \\ q(z) &= q_0 \, \frac{l}{2\pi} \sin z \\ \dot{m}_+ &= q_0 \, \frac{l}{2\pi} \int\limits_0^\pi \sin z dz = q_0 l \, / \, \pi \\ \dot{m}_- &= q_0 \, \frac{l}{2\pi} \int\limits_{-\pi}^0 \sin z dz = -q_0 l \, / \, \pi \end{split}$$





Mean flow for suction-blowing system

 $(m_{+}=6.75 g/s)$

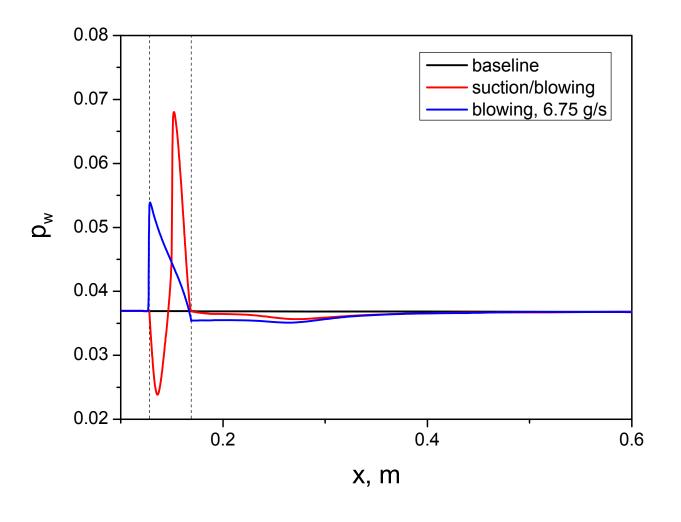








Wall pressure distribution for suction-blowing system (m,=6.75 g/s)

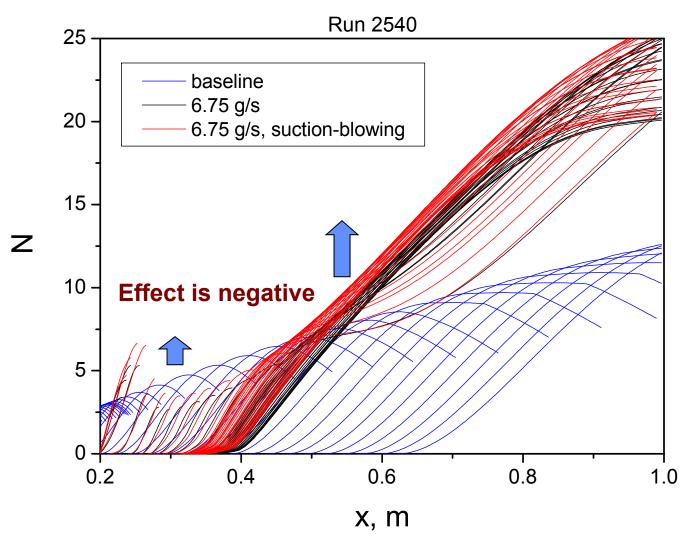








N-factors for suction-blowing system (m₊=6.75 g/s)









Conclusions

- Injection induces a cold dead-flow layer in the downstream relaxation region
- The near-wall flow behaves as a wave guide which can support several unstable modes of acoustic type
 - The most unstable is the Mack second mode
 - The phase speeds of instability are close to those of slow acoustic waves in the free-stream
 - Instability frequencies are several times smaller than in the no injection case
 - This may lead to dramatic increase of receptivity to free-stream noise





Conclusions (cont'd)

- The e^N computations for baseline configuration showed
 - Injection leads to destabilization of the near-field region, stabilization of the mid-field relaxation region, and destabilization of the far-field relaxation region
 - The level of these effects essentially depend on the injected mass flow rate
- The injector shaping considered
 - Does not stabilize the near-field flow at sufficiently large injection rates
- For relatively small injection rates the shaping produces a significant stabilization effect in the mid- and far-field relaxation regions
- The suction-blowing of zero mass addition destabilizes the flow in the whole relaxation region



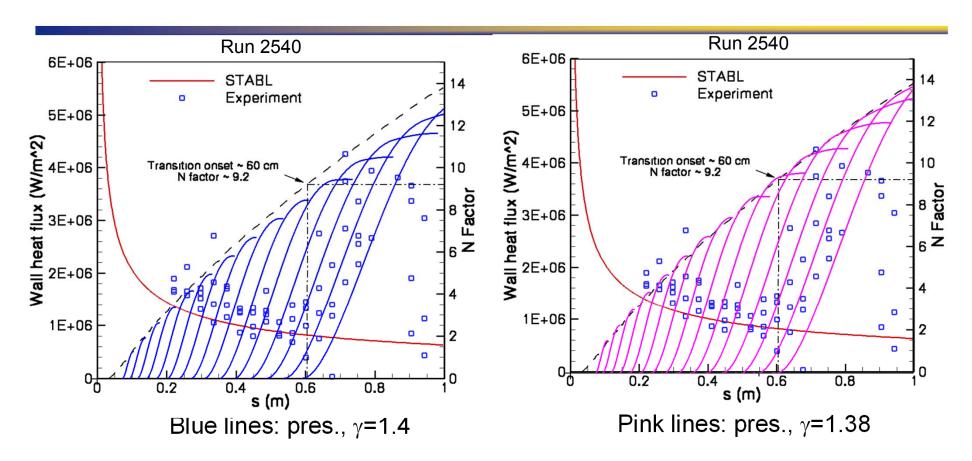


Backup





Stability analysis (cont'd)



With small correction of γ , N-factors predicted by the perfect-gas model are close to N-factors predicted by STABL*

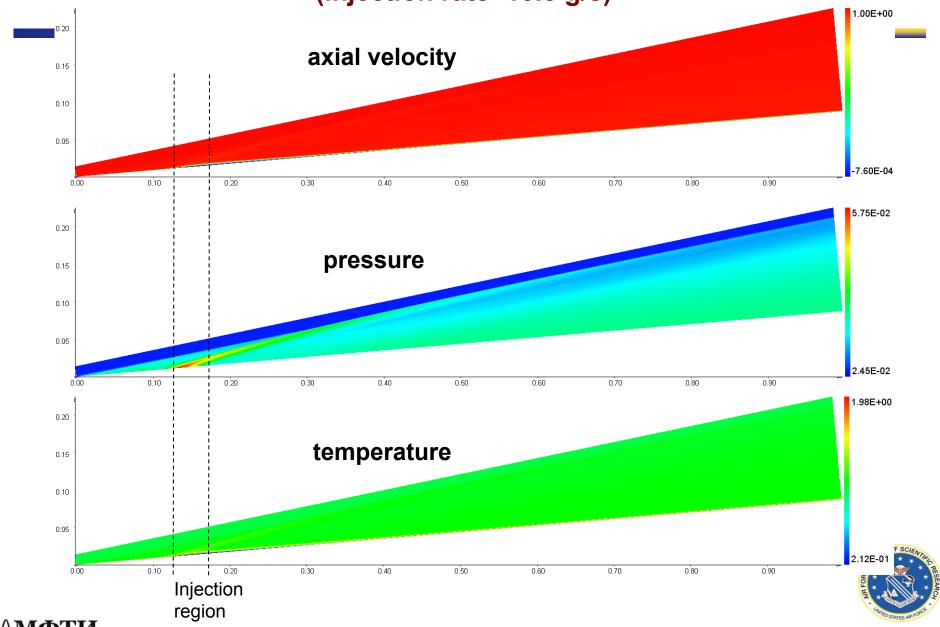




^{*}Wagnild, R.M. et al. AIAA-2010-1244

Mean flow for baseline configuration

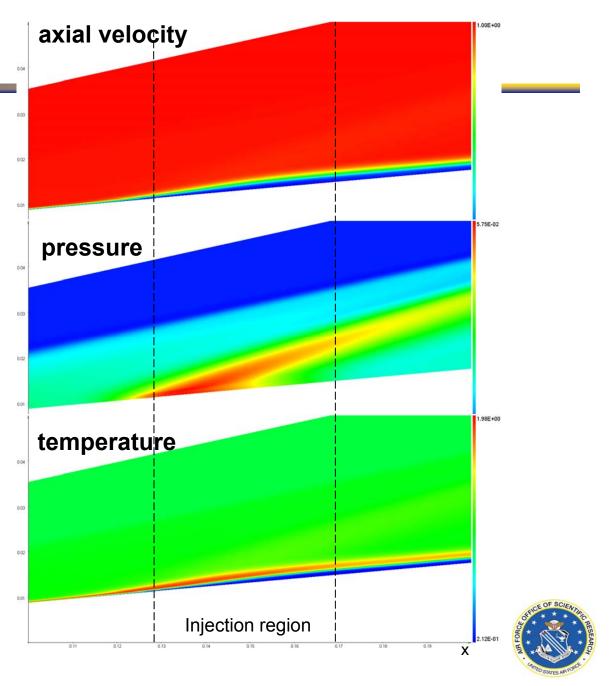






Mean flow near injection

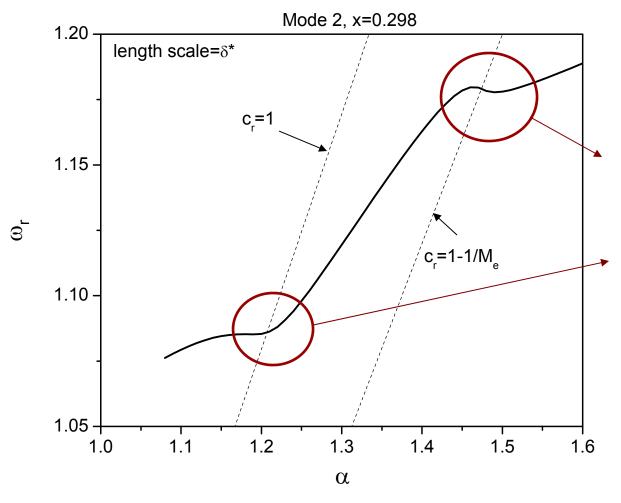
baseline configuration injection rate=13.5 g/s







It is not easy to convert temporal growth rates to spatial ones



Gaster transformation

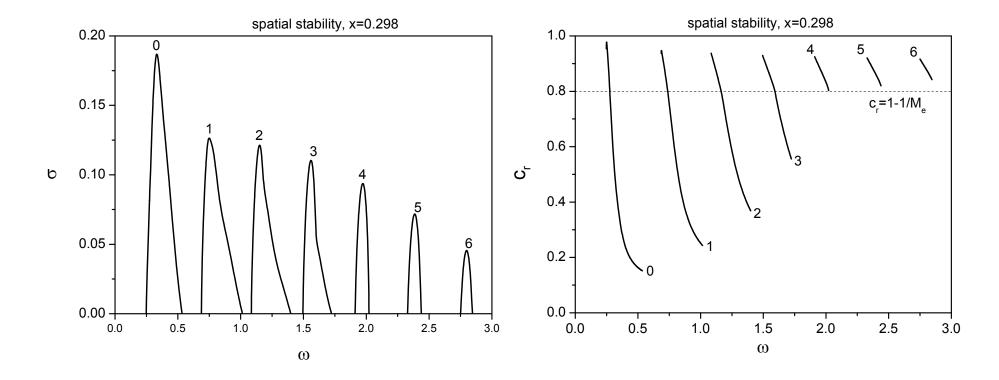
$$lpha_{_{i}}=-rac{\omega_{_{i}}}{V_{_{g}}}$$
 $V_{_{g}}=d\omega_{_{r}}/\,dlpha$

does not work here



Spatial stability analysis in the relaxation region

(injection rate=13.5 g/s, x=0.3)



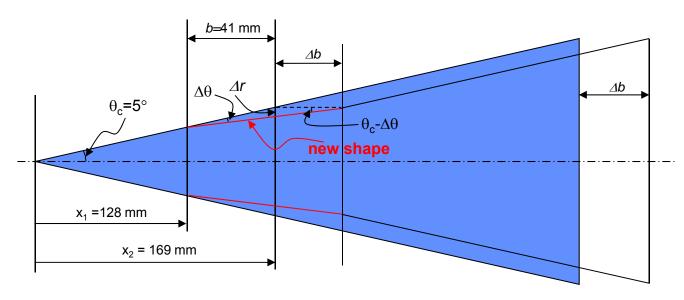
- Mode 0 (Mack second mode) is most unstable
- Its instability is observed at low phase speeds







Injector of conical shape



5-deg half-angle sharp cone with the injector having the slope $\theta = \theta_c - \Delta \theta$

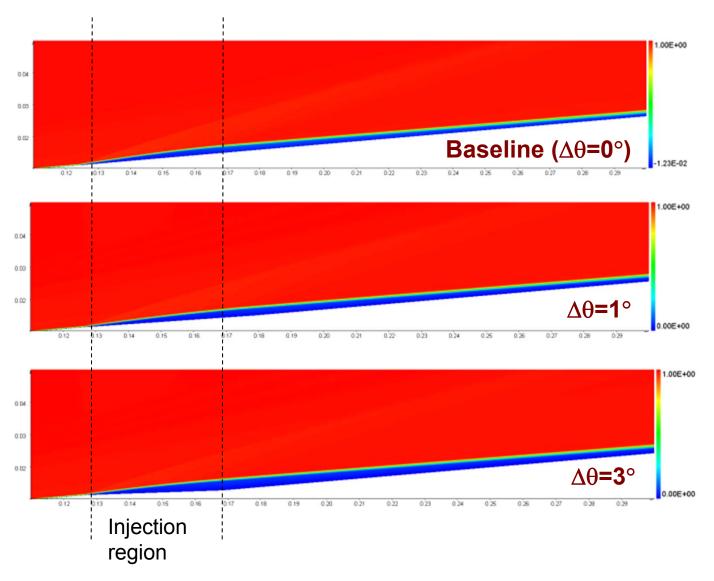
$$\begin{split} \Delta r &\approx b [\tan \theta_c - \tan (\theta_c - \Delta \theta)] \approx b \Delta \theta \\ \Delta b &= \frac{\Delta r}{\tan (\theta_c - \Delta \theta)} \approx \frac{\Delta r}{\tan \theta_c} \end{split}$$





Mean-flow axial velocity for conical injectors

(injection rate 13.5 g/s)

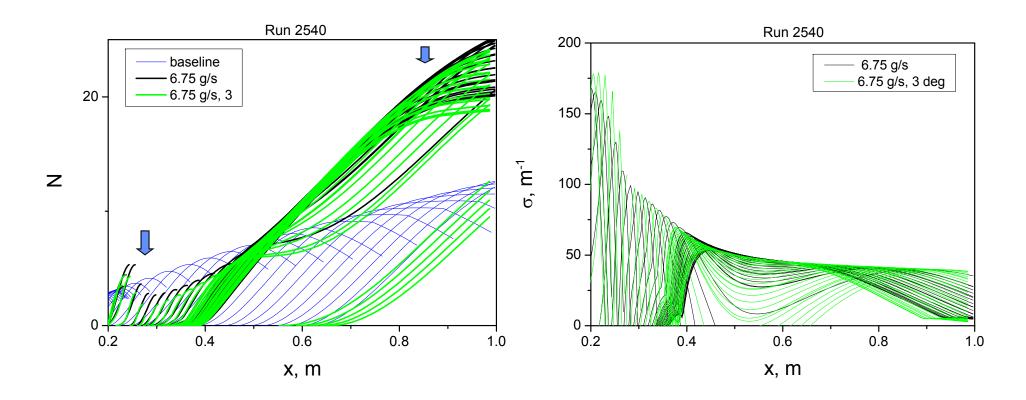








Shaping of $\Delta\theta$ =3° with injection 6.75 g/s



Conical injector with $\Delta\theta$ =3° shaping

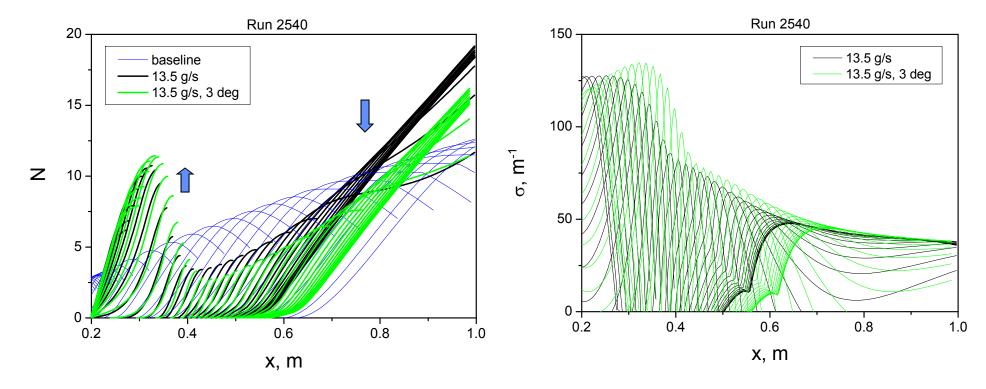
- Slightly stabilizes flow in the near-field relaxation region
- Almost zero effect in the far-field relaxation region







Shaping of $\Delta\theta$ =3° with injection 13.5 g/s



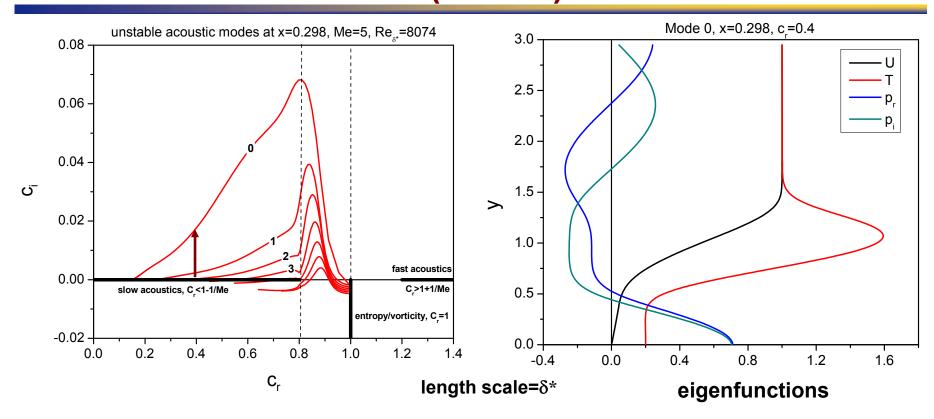
Conical injector with $\Delta\theta$ =3° shaping

- Slightly destabilizes flow in the near-field relaxation region
- Stabilizes flow in the far-field relaxation region





We are dealing with acoustic instability (cont'd)



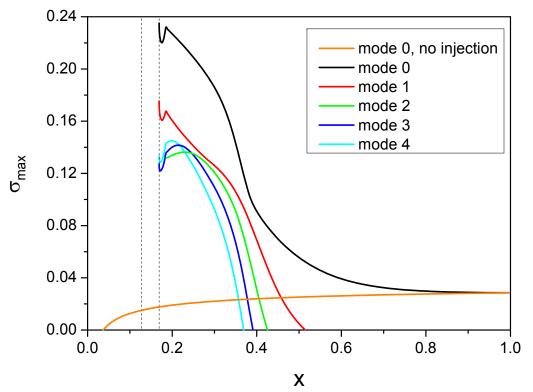
- Phase speeds of unstable modes are close to those of slow acoustic waves
- Resonant interaction can enhance receptivity to slow free-stream noise
- Instability is observed at low frequencies where free-stream noise is higher



THE AIR FORGE REMARKS LANDOFASCRY

Maximal growth rates in the relaxation region

(injection with 13.5 g/s)



- The most unstable mode is Mack second mode (mode 0)
- Unstable x-region decreases with the mode number

length scale= δ^*

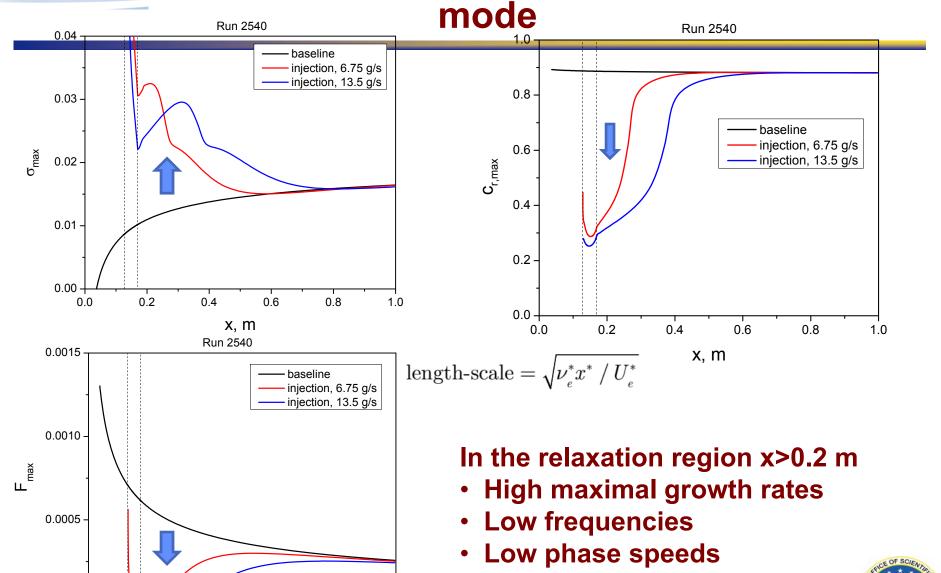
$$\sigma_{\text{max}} = -\alpha_{i,\text{max}} = \max_{\omega} \left[-\alpha_{i}(\omega) \right]$$

Further analysis is focused on the Mack second mode





Maximal growth rates of Mack second





0.0000 -

0.4

0.6

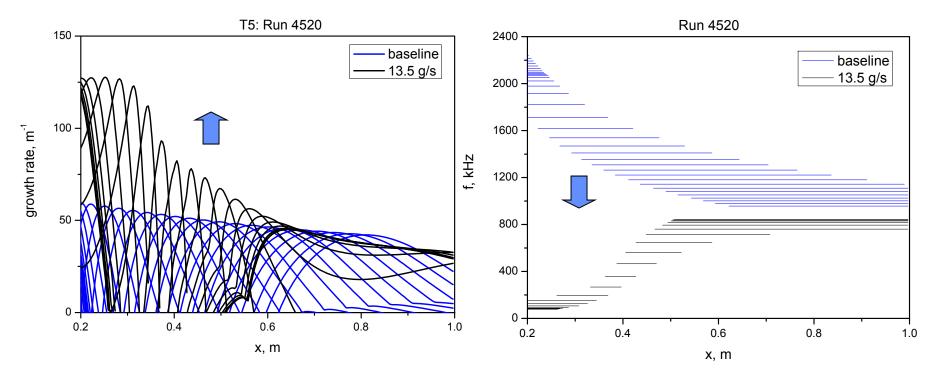
8.0

1.0

x, m Distribution A: Approved for Public Release; Distribution Unlimited



Injection affects growth rates and frequencies in the relaxation region



Maximal growth rates are increased Unstable region is

- narrowed down for x<0.6
- widened for x>0.6

Frequencies are decreased







Maximal growth rates for cylindrical injector

(various injection rates)

